

Final examination, 23 April 2008

All aids are allowed, except personal computer and personal assistance. The exam consists of 3 questions, which have equal weight (*10 points each*) and should all be answered; further detail about the points is given for specific parts of each question. The duration of the exam is 3 hours.

Generally, all statistical models used should be specified, and to such detail that it is clear which terms are present and in which form. Your answers should generally (unless specified otherwise) be based on the information provided: the study descriptions, data listings and computer listing. Nevertheless, if at some point you think it is necessary to carry out additional analysis in statistical software, explain carefully the purpose of your proposed analysis and how you would implement it in Minitab or Stata.

Question 1.

Most universities teach many sections of introductory calculus, and faculty are constantly looking for a method to evaluate students consistently across sections. An exam service claims that it can supply different exams that consistently evaluate students. Some faculty are sceptical of this claim, in part because they believe that the text(book) used may affect how specific exams work. Three math departments at three different universities (A, B, C) propose the following experiment. Three random final exams are obtained from the service (E1, E2, E3). At each of the universities, the three exams will be used in random order in the fall, winter, and spring quarters. The three universities all use the same two texts (T1, T2). Sections of the courses within each quarter and university will be divided at random into two groups, with half of the sections using text T1 and the other half using text T2. At the end of the year, the mean test scores were tallied with the following results.

Mean test score	Exam E1		Exam E2		Exam E3	
University	Text T1	Text T2	Text T1	Text T2	Text T1	Text T2
A	81	87	79	85	70	78
B	84	82	81	81	83	84
C	87	98	82	93	86	90

Use the description of the study and the information contained in the subsequent Minitab and Stata listings (for Question 1) to answer to the following questions.

- A) (*5 points*) Describe the experimental design in statistical terms, and formulate a statistical model that properly reflects the experimental design. Explain the meaning of each term in your model. (*Hint*: It may be helpful to display the experimental design or the data structure by a sketch/diagram.)
- B) (*3 points*) Use the attached output from statistical software to assess, by means of estimates or statistical tests, the different effects of your model. Draw conclusions about the questions of interest that motivated the study (as described above).
- C) (*2 points*) In continuation of the discussion in B), use the information provided to draw specific conclusions about how the specific exams, texts, and universities affected the exam scores.

Minitab listing for Question 1:

note: the Stata listing contains additional information

```
MTB > GLM 'score' = exam|text univ;
SUBC> Brief 2 ;
SUBC> EMS.
General Linear Model: score versus exam, text, univ
```

Factor	Type	Levels	Values
exam	fixed	3	E1, E2, E3
text	fixed	2	T1, T2
univ	fixed	3	A, B, C

Analysis of Variance for score, using Adjusted SS for Tests

Source	DF	Seq SS	Adj SS	Adj MS	F	P
exam	2	67.11	67.11	33.56	2.00	0.186
text	1	112.50	112.50	112.50	6.70	0.027
exam*text	2	1.33	1.33	0.67	0.04	0.961
univ	2	280.11	280.11	140.06	8.34	0.007
Error	10	167.89	167.89	16.79		
Total	17	628.94				

S = 4.09742 R-Sq = 73.31% R-Sq(adj) = 54.62%

Variance Components, using Adjusted SS

Source	Estimated Value
Error	16.79

```
MTB > GLM 'score' = exam|text univ|exam;
SUBC> Random 'univ';
SUBC> Brief 2 ;
SUBC> EMS.
General Linear Model: score versus exam, text, univ
```

Factor	Type	Levels	Values
exam	fixed	3	E1, E2, E3
text	fixed	2	T1, T2
univ	random	3	A, B, C

Analysis of Variance for score, using Adjusted SS for Tests

Source	DF	Seq SS	Adj SS	Adj MS	F	P
exam	2	67.11	67.11	33.56	1.63	0.303
text	1	112.50	112.50	112.50	7.88	0.031
exam*text	2	1.33	1.33	0.67	0.05	0.955
univ	2	280.11	280.11	140.06	6.81	0.051
exam*univ	4	82.22	82.22	20.56	1.44	0.328
Error	6	85.67	85.67	14.28		
Total	17	628.94				

S = 3.77859 R-Sq = 86.38% R-Sq(adj) = 61.41%

Variance Components, using Adjusted SS

Source	Estimated Value
univ	19.917
exam*univ	3.139
Error	14.278

```
MTB > GLM 'score' = exam|text univ|text;
SUBC> Random 'univ';
SUBC> Brief 2 ;
SUBC> EMS.
```

General Linear Model: score versus exam, text, univ

Factor	Type	Levels	Values
exam	fixed	3	E1, E2, E3
text	fixed	2	T1, T2
univ	random	3	A, B, C

Analysis of Variance for score, using Adjusted SS for Tests

Source	DF	Seq SS	Adj SS	Adj MS	F	P
exam	2	67.11	67.11	33.56	2.66	0.130
text	1	112.50	112.50	112.50	3.36	0.208
exam*text	2	1.33	1.33	0.67	0.05	0.949
univ	2	280.11	280.11	140.06	4.18	0.193
text*univ	2	67.00	67.00	33.50	2.66	0.130
Error	8	100.89	100.89	12.61		
Total	17	628.94				

S = 3.55121 R-Sq = 83.96% R-Sq(adj) = 65.91%

Variance Components, using Adjusted SS

Source	Estimated Value
univ	17.759
text*univ	6.963
Error	12.611

Stata listing for Question 1:

note: the Minitab listing contains additional information

```
. table text exam, contents(mean score ) row col
```

text	exam			
	E1	E2	E3	Total
T1	84	80.6667	79.6667	81.4444
T2	89	86.3333	84	86.4444
Total	86.5	83.5	81.8333	83.9444

```
. table univ exam, contents(mean score ) col
```

univ	exam			
	E1	E2	E3	Total
A	84	82	74	80
B	83	81	83.5	82.5
C	92.5	87.5	88	89.3333

```
. table text univ, contents(mean score )
```

text	univ		
	A	B	C
T1	76.6667	82.6667	85
T2	83.3333	82.3333	93.6667

```
. encode univ, gen(Univ)
. encode exam, gen(Exam)
. encode text, gen(Text)
```

```
. anova score Exam Text Exam*Text Univ
```

Number of obs = 18 R-squared = 0.7331
 Root MSE = 4.09742 Adj R-squared = 0.5462

Source	Partial SS	df	MS	F	Prob > F
Model	461.055556	7	65.8650794	3.92	0.0255
Exam	67.1111111	2	33.5555556	2.00	0.1861
Text	112.5	1	112.5	6.70	0.0270
Exam*Text	1.33333333	2	.666666667	0.04	0.9612
Univ	280.111111	2	140.055556	8.34	0.0074
Residual	167.888889	10	16.7888889		
Total	628.944444	17	36.996732		

. anova score Exam Univ / Exam*Univ Text Exam*Text

Number of obs = 18 R-squared = 0.8638
 Root MSE = 3.77859 Adj R-squared = 0.6141

Source	Partial SS	df	MS	F	Prob > F
Model	543.277778	11	49.3888889	3.46	0.0700
Exam	67.1111111	2	33.5555556	1.63	0.3032
Univ	280.111111	2	140.055556	6.81	0.0515
Exam*Univ	82.2222222	4	20.5555556		
Text	112.5	1	112.5	7.88	0.0309
Exam*Text	1.33333333	2	.666666667	0.05	0.9547
Residual	85.6666667	6	14.2777778		
Total	628.944444	17	36.996732		

. anova score Text Univ / Text*Univ Exam Exam*Text

Number of obs = 18 R-squared = 0.8396
 Root MSE = 3.55121 Adj R-squared = 0.6591

Source	Partial SS	df	MS	F	Prob > F
Model	528.055556	9	58.6728395	4.65	0.0207
Text	112.5	1	112.5	3.36	0.2083
Univ	280.111111	2	140.055556	4.18	0.1930
Text*Univ	67	2	33.5		
Exam	67.1111111	2	33.5555556	2.66	0.1301
Exam*Text	1.33333333	2	.666666667	0.05	0.9488
Residual	100.888889	8	12.6111111		
Total	628.944444	17	36.996732		

Questions 2-3.

Not shown.